

# Physical Biology of the Cell

PBoC@MOLPIT

Peter I Belobrov  
<http://molpit.com>

11/1/2014

# Robert Brooks Phillips

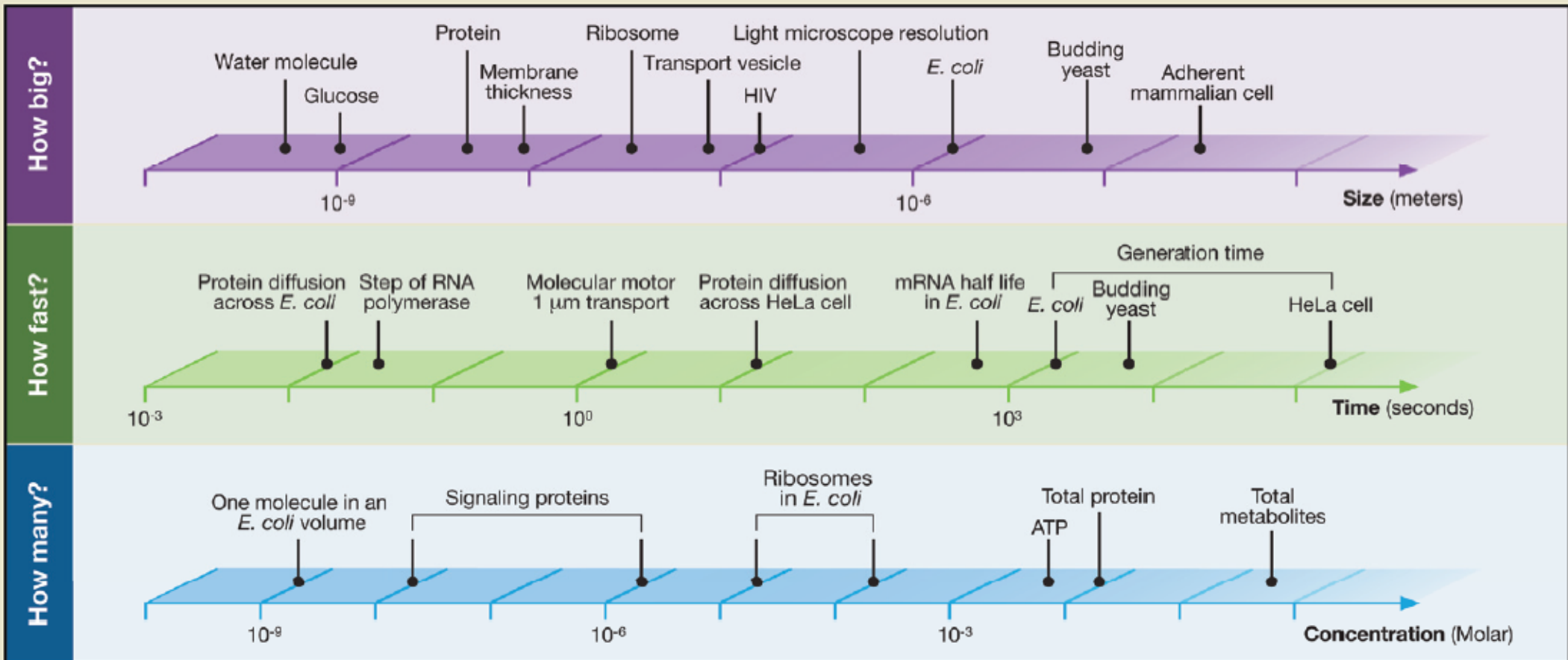
- Rob Phillips Group: **Physical Biology of the Cell**
  - <http://www.rpgroup.caltech.edu/>
- Rob Phillips, Jane Kondev, Julie Theriot. Physical Biology of the Cell [1 ed.] Garland Science. 2008. 826 p.
- Robert Brooks Phillips, Jane Kondev, Julie Theriot. Physical Biology of the Cell. Taylor & Francis Group, 2009, 807 p. (reprint ed.)
- Rob Phillips, Jane Kondev, Julie Theriot, Nigel Orme, Herman Garcia. Physical biology of the cell [2 nd.] Garland Science. 2013. 1040 p.

# <http://microsite.garlandscience.com/pboc2/> Home - Physical Biology of the Cell

- <http://microsite.garlandscience.com/pboc2/data.html>
  - Data 164K - Physical Biology of the Cell
- <http://microsite.garlandscience.com/pboc2/hints.html>
  - Hints 468K - Physical Biology of the Cell
- <http://microsite.garlandscience.com/pboc2/matlab.html>
  - Mathematica® & Matlab® Codes 343K
- <http://microsite.garlandscience.com/pboc2/powerpoints.html>
  - PowerPoints® 263M - Physical Biology of the Cell
- <http://microsite.garlandscience.com/pboc2/jpegs.html>
  - JPEGs 204M - Physical Biology of the Cell
- <http://microsite.garlandscience.com/pboc2/videos.html>
  - Videos 68M - Physical Biology of the Cell ! Nice & Useful video edu !

# SnapShot: key numbers in biology

- Uri Moran, Rob Phillips, Ron Milo. SnapShot: key numbers in biology // *Cell*, **141** (7), 1262-1262 (2010).



# Uri Moran, Rob Phillips, Ron Milo. SnapShot: key numbers in biology // *Cell*, 141 (7), 1262-1262 (2010).

## Cell size

**Bacteria (*E. coli*):**  $\approx 0.7\text{-}1.4\ \mu\text{m}$  diameter,  $\approx 2\text{-}4\ \mu\text{m}$  length,  $\approx 0.5\text{-}5\ \mu\text{m}^3$  in volume;  $10^8\text{-}10^9$  cell/ml for culture with  $\text{OD}_{600} \approx 1$

**Yeast (*S. cerevisiae*):**  $\approx 3\text{-}6\ \mu\text{m}$  diameter  $\approx 20\text{-}160\ \mu\text{m}^3$  in volume

**Mammalian cell volume:**  $100\text{-}10,000\ \mu\text{m}^3$ ; HeLa cell:  $500\text{-}5000\ \mu\text{m}^3$  (adhering to slide  $\approx 15\text{-}30\ \mu\text{m}$  diameter)

## Length scales inside cells

**Nucleus volume:**  $\approx 10\%$  of cell volume

**Cell membrane thickness:**  $\approx 4\text{-}10\ \text{nm}$

**"Average" protein diameter:**  $\approx 3\text{-}6\ \text{nm}$

**Base pair:**  $2\ \text{nm}$  (D)  $\times$   $0.34\ \text{nm}$  (H)

**Water molecule diameter:**  $\approx 0.3\ \text{nm}$

## Energetics

**Membrane potential**  $\approx 70\text{-}200\ \text{mV} \rightarrow 2\text{-}6\ k_B T$  per electron ( $k_B T \equiv$  thermal energy)

**Free energy ( $\Delta G$ ) of ATP hydrolysis under physiological conditions**

$\approx 40\text{-}60\ \text{kJ/mol} \rightarrow \approx 20\ k_B T$ /molecule ATP; ATP molecules required during an *E. coli* cell cycle  $\approx 10\text{-}50 \times 10^9$

**$\Delta G^\circ$  resulting in order of magnitude ratio between product and reactant concentrations:**

$\approx 6\ \text{kJ/mol} \approx 60\ \text{meV} \approx 2\ k_B T$

## Concentration

**Concentration of 1 nM:**

in *E. coli*  $\approx 1$  molecule/cell;  
in HeLa cells  $\approx 1000$  molecules/cell

**Characteristic concentration for a signaling protein:**  $\approx 10\ \text{nM}\text{-}1\ \mu\text{M}$

**Water content:**  $\approx 70\%$  by mass; general elemental composition (dry weight) of *E. coli*:  $\approx \text{C}_4\text{H}_7\text{O}_2\text{N}_1$ ; Yeast:  $\approx \text{C}_6\text{H}_{10}\text{O}_3\text{N}_1$

**Composition of *E. coli* (dry weight):**  $\approx 55\%$  protein,  $20\%$  RNA,  $10\%$  lipid,  $15\%$  other

**Protein concentration:**  $\approx 100\ \text{mg/ml} = 3\ \text{mM}$ .  $10^6\text{-}10^7$  per *E. coli* (depending on growth rate); Total metabolites (MW  $< 1\ \text{kDa}$ )  $\approx 300\ \text{mM}$

**Division, replication, transcription, translation, and degradation rates** at  $37^\circ\text{C}$  with a temperature dependence (Q10) of  $\approx 2\text{-}3$

**Cell cycle time** (exponential growth in rich media): *E. coli*  $\approx 20\text{-}40\ \text{min}$ ; budding yeast  $70\text{-}140\ \text{min}$ ; HeLa human cell line:  $15\text{-}30\ \text{hr}$

**Rate of replication by DNA polymerase:**

*E. coli*  $\approx 200\text{-}1000$  bases/s; human  $\approx 40$  bases/s. Transcription by RNA polymerase  $10\text{-}100$  bases/s

**Translation rate by ribosome:**  $10\text{-}20\ \text{aa/s}$

**Degradation rates (proliferating cells):**

mRNA half life  $<$  cell cycle time; protein half life  $\approx$  cell cycle time

## Diffusion and catalysis rate

**Diffusion coefficient for an "average" protein:** in cytoplasm  $D \approx 5\text{-}15\ \mu\text{m}^2/\text{s} \rightarrow \approx 10\ \text{ms}$  to traverse an *E. coli*  $\rightarrow \approx 10\ \text{s}$  to traverse a mammalian HeLa cell; small metabolite in water  $D \approx 500\ \mu\text{m}^2/\text{s}$

**Diffusion-limited on-rate for a protein:**  $\approx 10^8\text{-}10^9\ \text{s}^{-1}\text{M}^{-1} \rightarrow$  for a protein substrate of concentration  $\approx 1\ \mu\text{M}$  the diffusion-limited on-rate is  $\approx 100\text{-}1000\ \text{s}^{-1}$  thus limiting the catalytic rate  $k_{\text{cat}}$

## Genome sizes and error rates

**Genome size:**

*E. coli* (enterobacteria)  $\approx 5\ \text{Mbp}$   
*S. cerevisiae* (budding yeast)  $\approx 12\ \text{Mbp}$   
*C. elegans* (nematode)  $\approx 100\ \text{Mbp}$   
*D. melanogaster* (fruit fly)  $\approx 120\ \text{Mbp}$   
*A. thaliana* (plant)  $\approx 120\ \text{Mbp}$   
*M. musculus* (mouse)  $\approx 2.5\ \text{Gbp}$   
*H. sapiens* (human)  $\approx 2.9\ \text{Gbp}$   
*T. aestivum* (wheat)  $\approx 16\ \text{Gbp}$

**Number of protein-coding genes:**

*E. coli*  $\approx 4000$ ; *S. cerevisiae*  $\approx 6000$ ; *C. elegans*, *A. thaliana*, *M. musculus*, *H. sapiens*  $\approx 20,000$

**Mutation rate in DNA replication:**

$\approx 10^{-8}\text{-}10^{-10}$  per bp

**Misincorporation rate:**

transcription  $\approx 10^{-4}\text{-}10^{-5}$  per nucleotide  
translation  $\approx 10^{-3}\text{-}10^{-4}$  per amino acid

# Key Numbers for Cell Biologists

- <http://www.bionumbers.org/> =>
  - <http://bionumbers.hms.harvard.edu/KeyNumbers.aspx>
- Cell size (1-3)
- Length Scales Inside Cells (4-8)
- Division, Replication, Transcription, Translation & Degradation Rates (9-12)
- Concentration (13-17)
- Energetics (18-20)
- Diffusion and Catalysis Rate (21, 22)
- Genome sizes & Error Rates (23-26)

## Cell size

1. Bacteria (*E. coli*):  $\approx 0.7\text{-}1.4\ \mu\text{m}$  diameter,  $\approx 2\text{-}4\ \mu\text{m}$  length,  $\approx 0.5\text{-}5\ \mu\text{m}^3$  in volume;  $10^8\text{-}10^9$  cell/ml for culture with  $\text{OD}_{600}\approx 1$
2. Yeast (*S. cerevisiae*):  $\approx 3\text{-}6\ \mu\text{m}$  diameter,  $\approx 20\text{-}160\ \mu\text{m}^3$  in volume
3. Mammalian cell volume:  $100\text{-}10000\ \mu\text{m}^3$ ; Hela:  $500\text{-}5000\ \mu\text{m}^3$  (adherent on slide  $\approx 15\text{-}30\ \mu\text{m}$  diameter)

## Length Scales Inside Cells

4. Nucleus volume  $\approx 10\%$  of cell volume
5. Cell membrane thickness  $\approx 4\text{-}10\ \text{nm}$
6. "Average" protein diameter  $\approx 3\text{-}6\ \text{nm}$
7. Base pair:  $2\ \text{nm}$  (D) x  $0.34\ \text{nm}$  (H)
8. Water molecule diameter  $\approx 0.3\ \text{nm}$

## Division, Replication, Transcription, Translation & Degradation Rates

at  $37^\circ\text{C}$  with a temperature dependence  $Q_{10}$  of  $\approx 2\text{-}3$

9. Cell cycle time (exponential growth in rich media): *E. coli*  $\approx 20\text{-}40\ \text{min}$ ; yeast  $70\text{-}140\ \text{min}$ ; human cell line (Hela):  $15\text{-}30\ \text{hours}$
10. Rate of replication by DNA polymerase *E. coli*  $\approx 200\text{-}1000\ \text{bases/s}$ ; human  $\approx 40\ \text{bases/s}$ . Transcription by RNA polymerase  $10\text{-}100\ \text{bases/s}$
11. Translation rate by ribosome  $10\text{-}20\ \text{aa/s}$
12. Degradation rates (proliferating cells): mRNA half life  $<$  cell cycle time; protein half life  $\geq$  cell cycle time

## Concentration

13. Concentration of  $1\ \text{nM}$  in: *E. coli* is  $\approx 1$  molecule/cell; Hela  $\approx 1,000$  molecules/cell
14. Characteristic concentration for a signaling protein  $\approx 10\ \text{nM}\text{-}1\ \mu\text{M}$
15. Water content:  $\approx 70\%$  by mass; General elemental composition (dry weight) of *E. coli*:  $\approx \text{C}_4\text{H}_7\text{O}_2\text{N}_1$ ; Yeast  $\approx \text{C}_6\text{H}_{10}\text{O}_3\text{N}_1$
16. Composition of *E. coli* (dry weight):  $\approx 55\%$  protein,  $20\%$  RNA,  $10\%$  lipids,  $15\%$  others
17. Protein conc.  $\approx 100\ \text{mg/ml} = 3\ \text{mM}$ .  $10^6\text{-}10^7$  per *E. coli* (depending on growth rate); Total metabolites (MW $<$ 1kD)  $\approx 300\ \text{mM}$

## Energetics

18. Membrane potential  $\approx 70\text{-}200\ \text{mV}$   $\rightarrow$   $2\text{-}6\ k_B T$  per electron ( $k_B T \equiv$  thermal energy)
19. Free energy ( $\Delta G$ ) of ATP hydrolysis under physiological conditions  $\approx 40\text{-}60\ \text{kJ/mole}$   $\rightarrow \approx 20 k_B T$ /molecule ATP; ATP molecules required to make an *E. coli* cell  $\approx 10\text{-}50 \times 10^9$
20.  $\Delta G^0$  resulting in order of magnitude ratio between products and reactants concentrations:  $\approx 6\ \text{kJ/mol}$   $\approx 60\ \text{meV}$   $\approx 2\ k_B T$

Useful biological numbers extracted from the literature. Numbers and ranges should only serve as "rule of thumb" values. References are in the online annotated version at the BioNumbers website. Consult website and original references to learn about the details of the system under study including growth conditions, method of measurement, etc.

## Diffusion and Catalysis Rate

21. Diffusion coefficient for an "average" protein: in cytoplasm  $D \approx 5\text{-}15\ \mu\text{m}^2/\text{s}$   $\rightarrow \approx 10$  millisecon to traverse an *E. coli*  $\rightarrow \approx 10\ \text{s}$  to traverse a mammalian (Hela) cell; small metabolite in water  $D \approx 500\ \mu\text{m}^2/\text{s}$
22. Diffusion limited on-rate for characteristic protein  $\approx 10^8\text{-}10^9\ \text{s}^{-1}\text{M}^{-1}$   $\rightarrow$  for a protein substrate of concentration  $\approx 1\ \mu\text{M}$  the diffusion limited on-rate is  $\approx 100\text{-}1000\ \text{s}^{-1}$  thus limiting the catalytic rate  $k_{\text{cat}}$

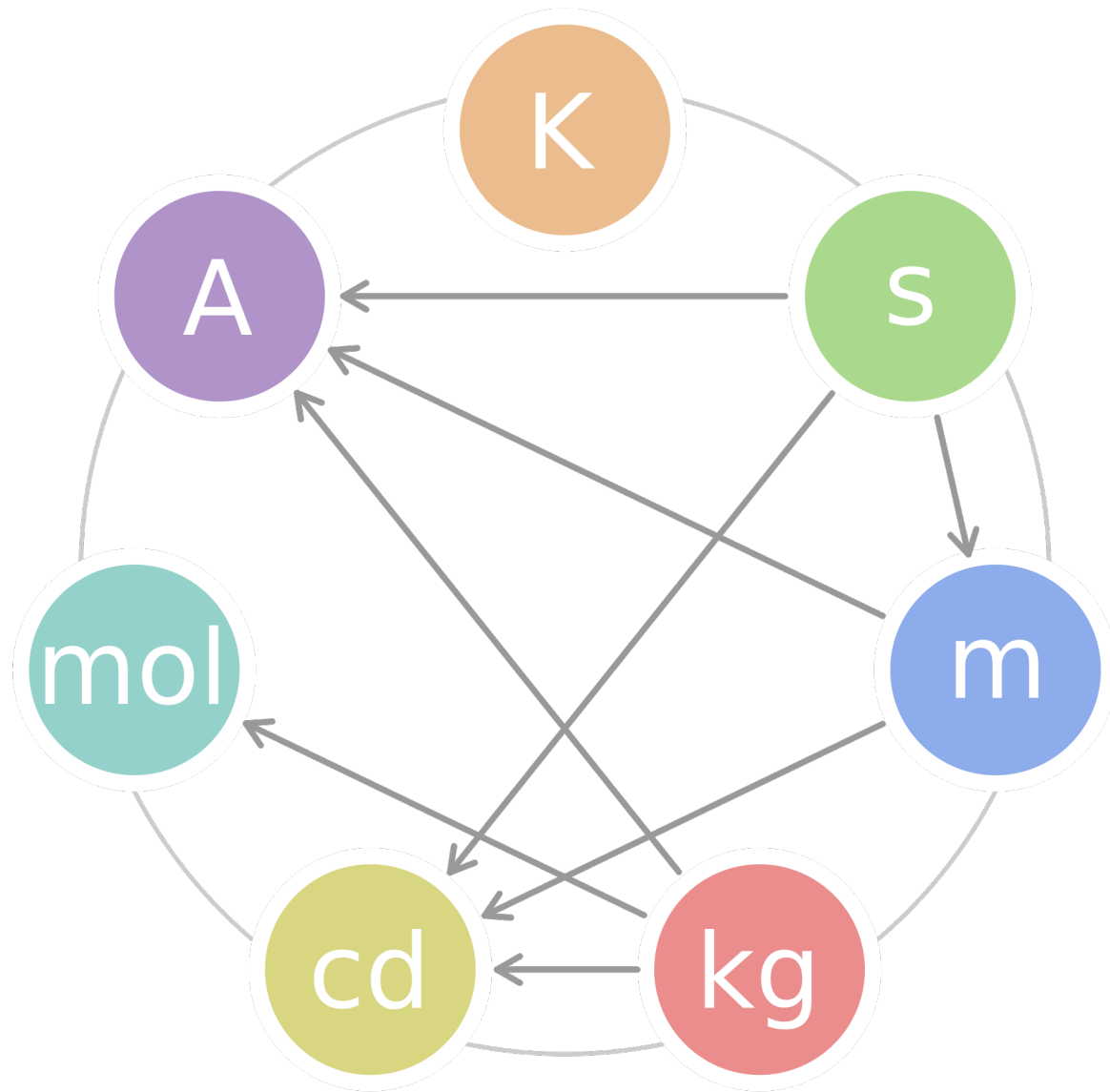
## Genome sizes & Error Rates

23. Genome size: *E. coli*  $\approx 5\ \text{Mbp}$ ; *S. cerevisiae* (yeast)  $\approx 12\ \text{Mbp}$ ; *C. elegans* (nematode)  $\approx 100\ \text{Mbp}$ ; *D. melanogaster* (fruit fly)  $\approx 120\ \text{Mbp}$ ; *A. thaliana* (arabidopsis)  $\approx 120\ \text{Mbp}$ ; *M. musculus* (mouse)  $\approx 2.5\ \text{Gbp}$ ; *H. sapiens* (human)  $\approx 2.9\ \text{Gbp}$ ; *T. aestivum* (wheat)  $\approx 16\ \text{Gbp}$
24. Number of protein-coding genes: *E. coli*  $\approx 4,000$ ; *S. cerevisiae*  $\approx 6,000$ ; *C. elegans*, *A. thaliana*, *M. musculus*, *H. sapiens*  $\approx 20,000$
25. Mutation rate in DNA replication  $\approx 10^{-8}\text{-}10^{-10}$  per bp
26. Misincorporation rate: transcription  $\approx 10^{-4}$  per nucleotide; translation  $\approx 10^{-3}\text{-}10^{-4}$  per amino-acid

Click on a number to see full description and reference  
[www.BioNumbers.org](http://www.BioNumbers.org)

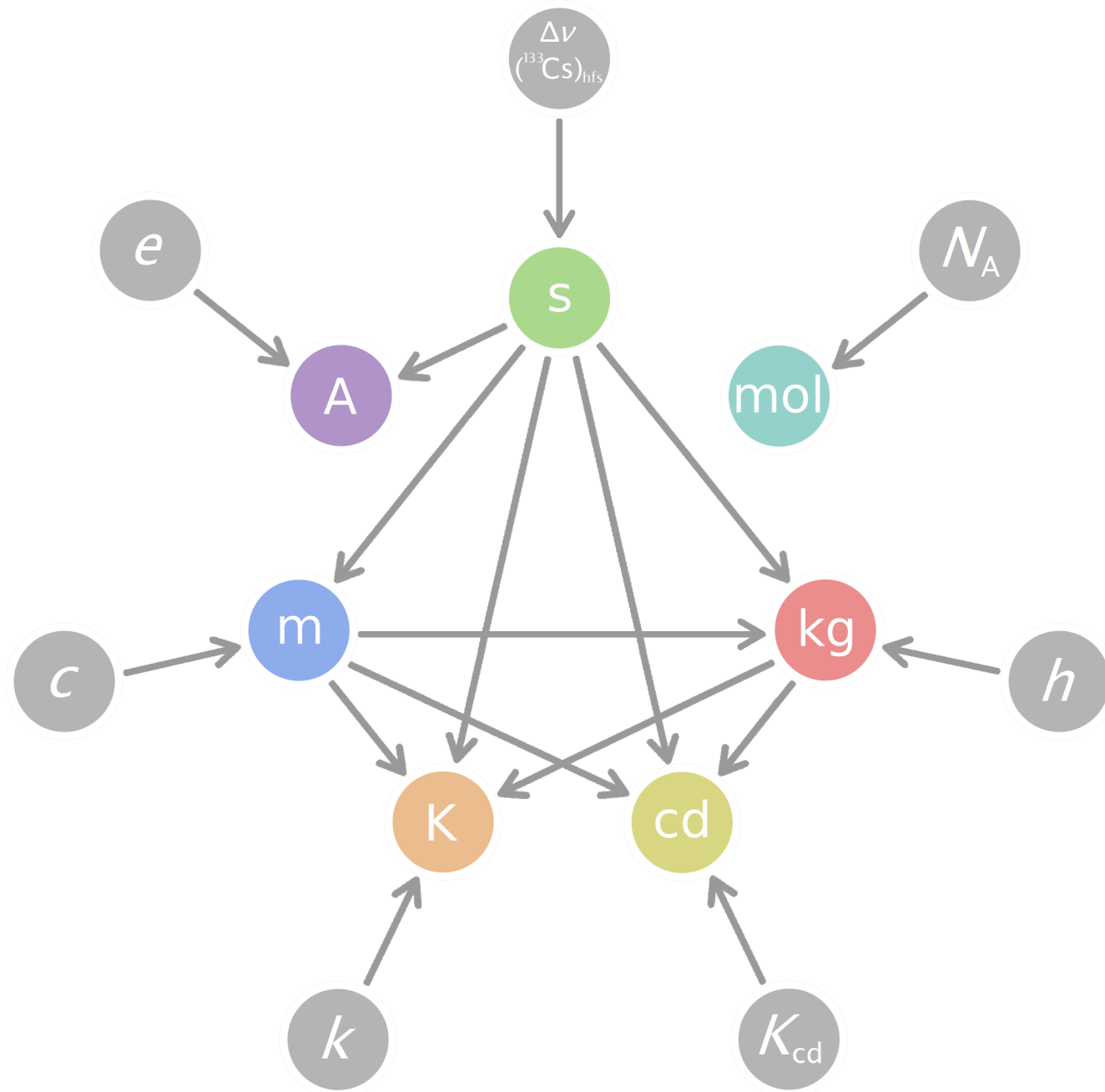
# Current (2013) SI System:

Dependence of base unit definitions on other base units





# Proposed «Quantum SI» System (2014)



# Biological measures & gauges

- From Key Numbers for Cell Biologists
- Towards BioMeasures & BioGauges
  - ? who, where, when
  - To make «Biological SI» System
- With Fundamental Biological Constant
  - Based on «Quantum SI» System
- Let's act together